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## MODELING OF ENERGETIC PARTICLE TRANSPORT AND ACCELERATION BY A BLAST WAVE PROPAGATING IN A SPIRAL MAGNETIC FIELD

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#### energetic particles in the Heliosphere



classical picture: e.g., Reames (1999)

(1) impulsive events localized source (flare) electron-rich <sup>3</sup>He-rich

(2) gradual events extended source (shock / CME) high ion flux lower e/p ratio

realistic transport models required to reconstruct particle properties at the Sun from spacecraft observations:

acceleration time scales, energy and charge spectra, PAD, relation to electromagnetic emission close to the Sun (radio, X-ray, gamma-ray) (3) mixed events – seed flare particles +shock-accelerated (Cane et al., 2003)

AU





### Blast wave in spiral magnetic field Parker, ApJ, 1961, 133, 1014



Simulations are performed in the de Hoffmann-Teller frame

$$B_r = B_0 \left(\frac{r_{\odot}}{r}\right)^2$$

$$B_{\varphi} = \frac{\Omega r_{\odot}}{U_{SW}} B_0 \left(\frac{r_{\odot}}{r}\right) \sin\theta$$

If  $r > R_{sh}$  – standard Parker field

If  $r = R_{sh} - \text{jump in } B_{\varphi}$ , if  $r < R_{sh}$  then

$$B_{\varphi} = B_0 \frac{\Omega r_{\odot}^2 S \sin\theta}{U_{SW} R_{sh}} \left(\frac{r}{R_{sh}}\right)^2$$

$$B_r$$
 – same as for  $r > R_{sh}$ 



#### Oblique shock



$$\mu_1^2 \geq 1 - \frac{B_1}{B_2}$$

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particles go from upstream to downstream and

$$\mu_2^2 = 1 - \frac{B_2}{B_1}(1 - \mu_1^2)$$

$$\mu_1^2 = 1 - \frac{B_1}{B_2}(1 - \mu_2^2)$$

particles go from downstream to upstream with changing PA

$$S = \frac{B_{z2}}{B_{z1}} = \frac{u_1}{u_2}$$

Reflection when particles go from upstream to downstream is added. If first adiabatic invariant is conserved than



The Fokker-Planck equation will be in this case:

$$\frac{\partial f}{\partial t} + \mu v \frac{\partial f}{\partial s} + \frac{1 - \mu^2}{2L} v \frac{\partial f}{\partial \mu} - \frac{\partial}{\partial \mu} D_{\mu\mu} \frac{\partial f}{\partial \mu} = q(s, \mu, t)$$

Stochastic differential equations for changes in  $\ {\it s}$  and  $\ {\it \mu}$ 

$$\vec{s}(t) = \mu v \ dt \ \vec{e_s} \qquad d\mu = \sqrt{D_{\mu\mu}} dW_{\mu}(t) + \left(\frac{v}{2L}(1-\mu^2) + \frac{\partial D_{\mu\mu}}{\partial\mu}\right) dt$$

$$D_{\mu\mu} = k_0(r, R) \{ |\mu|^{q-1} + H \} (1 - \mu^2)$$

The pitch angle diffusion coefficient

$$\frac{\partial b_i}{\partial x_i} \equiv -\frac{1}{L} = \frac{1}{B} \frac{dB}{d\xi}$$

Convection and energy changes are included implicitly through the transformation between fluid/magnetic field lines systems (Kocharov et al., 1998; Vainio, Kocharov, Laitinen, 2000).

# Depending on the parameters – profiles contain either 1 or 2 peaks at low energies



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Development of time profiles with radial distance



Effect of shock speed and compression ratio (left – also effect of dV is involved (will be shown separately below)



Figure 8. The dependence of profiles at 128 keV on the shock speed and compression ratio



#### Effect of dV and mean free path



Figure 9. The dependence of profiles at 128 keV on the value Figure 10. The dependence of profiles at 128 keV on the mean free path.



#### Two events which were considered for our modeling



Flare M2.8 September, 30, 13:08 UT ~ N19W91

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Contamination by electrons in proton channels

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$$\lambda_{||} = 0.02 \ (10E)^{\alpha} \quad \text{AU}$$

$$\alpha = 1/6$$

Upstream – radial mfp is const Downstream – parallel mfp is const

Quasi-linear theory of particleturbulence interaction gives E  $E^{1/4}$  or  $E^{1/6}$  depending on the type of the turbulence (Kraichnan's or Kolmogorov's)

CI



#### Flare C9.7 April, 4, 15:22 UT N16W66





 $\lambda = 0.03 \text{ AU}$ 

Upstream – radial mfp is const Downstream – parallel mfp is const

 $U_{SH}$  ~ 800 km/s S=3.3

Even considering mfp constant in energy gives too late arrival at energies below 4-6 MeV

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#### Changing $\lambda_{||}$

Close to the onset the mfp at low energies is higher than at high energies!

128 keV -- 0.12 - 0.08 - 0.015 AU

1 MeV -- 0.05 - 0.04 - 0.03 AU

6.7 MeV -- 0.04 - 0.03 - 0.02 AU

After some time after the injection the mfp is decreasing towards the shock

Unfortunately no single injection spectrum was obtained so far and no common rule

Nevertheless in principally it is possible to fit, assuming the energy dependence of the mfp obeying the resonance broadening

## CONCLUSIONS

- simulations for particles injected at the Sun together with a traveling interplanetary blast wave were performed
- these simulations resemble well the observed intensity—time profiles of ions in the energy ranges of hundreds of keV/nucleon to several MeV/nucleon in mixed SEP events
- in case of oblique geometry (blast waves in spiral magnetic field) the enhancements in time profiles of energetic particles are larger than for parallel geometry (the case of radial magnetic field)
- the energy dependence of the mean free path can either follow the law which follows from quasi-linear theory of particles-turbulence interaction or exhibit the opposite dependence, which is most likely related to the resonance broadening
- apparently in some cases the mean free path is decreasing towards the shock front

### Thanks for your attention !

